

*Cálculo del equilibrio líquido-vapor (dewpoint) de una mezcla de gas de síntesis y agua a alta presión (P = 30 atm).*

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*Se utiliza la ecuación de Redlich-Kwong modificada por De Santis & al. Ind. Eng. Chem. Proc. Des. Dev. 13, 1974*

*según el artículo Enthalpy and Dew Point Calculations for Aqueous Gas Mixtures Produced in Coal Gasification and Similar Processes*

*B. Rittmann, H. Knapp, J.M. Prausnitz, Ind. Eng. Chem. Proc. Des. Dev. 21, 1982.*

$$P = R \cdot T / (v - b) - a(T) / T^{1/2} v / (v + b)$$

	$b_i$	$a_{ij}$	$P_c$ (atm)	$T_c$ (K)
H2O	0,0146	35	218,3	647,4
CH4	45,8	190,7		
H2	$20,2 / (1 + 44,2 / (2,016 / T))$	$43,6 / (1 + 21,8 / (2,016 / T))$		quantum effects
CO	34,5	133		
CO2	0,0297	46,0	72,9	304,2
N2	0,02678	15,462	33,5	126,2
A	48,0	151,2		

*Para vapor de agua  $a(T) = (93,415 - 1,99798E4/T + 1,473169E7/T^2 + 7,47112E9/T^3)$  y  $a_0 = 35$*

*Su derivada es :  $da/dT = (1,99798E4/T^2 - 2 \cdot 1,473169E7/T^3 - 3 \cdot 7,47112E9/T^4)$*

*Para CO2 gas  $a(T) = (-7,97203 + 5,04354E4/T - 9,77329E6/T^2 + 5,19402E8/T^3)$  y  $a_0 = 46$*

*Su derivada es :  $da/dT = (-5,0435E4/T^2 + 2 \cdot 9,77329E6/T^3 - 3 \cdot 5,19402E8/T^4)$*

*El pseudoequilibrio en la fase gas de CO2+H2O :  $\ln K = -11,071 + 5953/T - 2746E3/T^2 + 464,6E6/T^3$*

*Los gases son 1= H2O, 2 = CH4, 3 = H2, 4 = CO, 5 = CO2, 6 = N2, 7 = A*

*Composición gaseosa inicial*

$$y_{0,1} = 0,3204 \quad \text{H2O}$$

$$y_{0,2} = 0,001785 \quad \text{CH4}$$

$$y_{0,3} = 0,3967 \quad \text{H2}$$

$$y_{0,4} = 0,0034 \quad \text{CO}$$

$$y_{0,5} = 0,1477 \quad \text{CO2}$$

$$y_{0,6} = 0,1298 \quad \text{N2}$$

$$y_{0,7} = 0 \quad \text{A}$$

$$b_1 = 0,0146$$

$$b_2 = 0,08664 \cdot 0,0820597 \cdot \frac{190,7}{45,8}$$

$$b_3 = 0,08664 \cdot 0,0820597 \cdot \left[ \frac{43,6}{1 + \frac{21,8}{2,016 \cdot T}} \right]$$

$$b_4 = 0,08664 \cdot 0,0820597 \cdot \frac{133}{34,5}$$

$$b_5 = 0,0297$$

$$b_6 = 0,02678$$

$$b_7 = 0,08664 \cdot 0,0820597 \cdot \frac{151,2}{48}$$

$$b_M = y_1 \cdot b_1 + y_2 \cdot b_2 + y_3 \cdot b_3 + y_4 \cdot b_4 + y_5 \cdot b_5 + y_6 \cdot b_6 + y_7 \cdot b_7$$

$$a_1 = 58,415 - \frac{19979,8}{T} + \frac{1,47316 \times 10^7}{T^2} + \frac{7,47112 \times 10^9}{T^3}$$

$$a_2 = 0,4275 \cdot 0,0820597^2 \cdot \frac{190,7^{2,5}}{45,8}$$

$$a_3 = 0,4275 \cdot 0,0820597^2 \cdot \left[ \frac{\left( \frac{43,6}{1 + \frac{21,8}{2,016 \cdot T}} \right)^{2,5}}{\frac{20,2}{1 + \frac{44,2}{2,016 \cdot T}}} \right]$$

$$a_4 = 0,4275 \cdot 0,0820597^2 \cdot \frac{133^{2,5}}{34,5}$$

$$a_5 = -53,97203 + \frac{50435,4}{T} - \frac{9,77329 \times 10^6}{T^2} + \frac{5,19402 \times 10^8}{T^3}$$

$$a_6 = 15,462$$

$$a_7 = 0,4275 \cdot 0,0820597^2 \cdot \frac{151,2^{2,5}}{48}$$

$$K = \exp \left[ \frac{\frac{4,646 \times 10^8}{T} - 2,746 \times 10^6}{T} + 5953 \right] - 11,071$$

$$dK = \frac{-5953}{T^2} + 2 \cdot \frac{2,746 \times 10^6}{T^3} - 3 \cdot \frac{4,646 \times 10^8}{T^4}$$

$$R = 0,0820597$$

$$a_M = \left[ y_1 \cdot 35^{0,5} + y_2 \cdot a_2^{0,5} + y_3 \cdot a_3^{0,5} + y_4 \cdot a_4^{0,5} + y_5 \cdot 46^{0,5} + y_6 \cdot a_6^{0,5} + y_7 \cdot a_7^{0,5} \right]^2 + y_1^2 \cdot a_1 + y_5^2 \cdot a_5 + y_1 \cdot y_5 \cdot R^2 \cdot T^{2,5} \cdot K$$

$$DT = \left[ \frac{19979,8}{T^2} - 2 \cdot \frac{1,47316 \times 10^7}{T^3} - 3 \cdot \frac{7,47112 \times 10^9}{T^4} \right] \cdot y_1^2 + \left[ \frac{-50435}{T^2} + 2 \cdot \frac{9,77329 \times 10^6}{T^3} - 3 \cdot \frac{5,19402 \times 10^8}{T^4} \right] \cdot y_5^2 + R^2 \cdot T^{1,5} \cdot K \cdot [2,5 + T \cdot dK] \cdot y_1 \cdot y_5$$

$$P = R \cdot \left[ \frac{T}{v - b_M} \right] - \left[ \frac{\frac{a_M}{v}}{T^{0,5}} \right]$$

$$\Delta h = \left[ P \cdot v - R \cdot T - \left( \left[ \frac{1,5 \cdot \frac{a_M}{\sqrt{T}} - DT \cdot \sqrt{T}}{b_M} \right] \cdot \ln \left[ \frac{v + b_M}{v} \right] \right) \right] \cdot \left| 101,325 \cdot \frac{\text{J/kmol}}{\text{atm} \cdot \text{l/kmol}} \right|$$

$$\ln [v_1] = \ln \left[ \frac{v}{v - b_M} \right] + \frac{b_1}{v - b_M} - \left[ \frac{\frac{2}{R}}{T^{1,5} \cdot b_M} \cdot \left( y_1 \cdot [35 + a_1] + y_2 \cdot [35 \cdot a_2]^{0,5} + y_3 \cdot [35 \right.$$

$$\cdot a_3]^{0,5} + y_4 \cdot [35 \cdot a_4]^{0,5} + y_5 \cdot [35 \cdot 46]^{0,5} + \frac{y_5}{2} \cdot R^2 \cdot T^{2,5} \cdot K + y_6 \cdot [35 \cdot a_6]^{0,5} + y_7 \cdot [35$$

$$\cdot a_7]^{0,5} \cdot \ln \left( \frac{v + b_M}{v} \right) \right] + a_M \cdot \frac{\frac{b_1}{R}}{T^{1,5} \cdot b_M^2} \cdot \left[ \ln \left( \frac{v + b_M}{v} \right) - \left( \frac{b_M}{v + b_M} \right) \right] - \ln \left[ P \cdot \frac{v}{R \cdot T} \right]$$

$$\ln [v_2] = \ln \left[ \frac{v}{v - b_M} \right] + \frac{b_2}{v - b_M} - \left[ \frac{\frac{2}{R}}{T^{1,5} \cdot b_M} \cdot \left( y_1 \cdot [a_2 \cdot 35]^{0,5} + y_2 \cdot a_2 + y_3 \cdot [a_2 \cdot a_3]^{0,5} + y_4 \right.$$

$$\cdot [a_2 \cdot a_4]^{0,5} + y_5 \cdot [a_2 \cdot 46]^{0,5} + y_6 \cdot [a_2 \cdot a_6]^{0,5} + y_7 \cdot [a_2 \cdot a_7]^{0,5} \cdot \ln \left( \frac{v + b_M}{v} \right) \right] + a_M$$

$$\cdot \frac{\frac{b_2}{R}}{T^{1,5} \cdot b_M^2} \cdot \left[ \ln \left( \frac{v + b_M}{v} \right) - \left( \frac{b_M}{v + b_M} \right) \right] - \ln \left[ P \cdot \frac{v}{R \cdot T} \right]$$

$$\ln [v_3] = \ln \left[ \frac{v}{v - b_M} \right] + \frac{b_3}{v - b_M} - \left[ \frac{\frac{2}{R}}{T^{1,5} \cdot b_M} \cdot \left( y_1 \cdot [a_3 \cdot 35]^{0,5} + y_2 \cdot [a_3 \cdot a_2]^{0,5} + y_3 \cdot a_3 + y_4 \right.$$

$$\cdot [a_3 \cdot a_4]^{0,5} + y_5 \cdot [a_3 \cdot 46]^{0,5} + y_6 \cdot [a_3 \cdot a_6]^{0,5} + y_7 \cdot [a_3 \cdot a_7]^{0,5} \cdot \ln \left( \frac{v + b_M}{v} \right) \right] + a_M$$

$$\cdot \frac{\frac{b_3}{R}}{T^{1,5} \cdot b_M^2} \cdot \left[ \ln \left( \frac{v + b_M}{v} \right) - \left( \frac{b_M}{v + b_M} \right) \right] - \ln \left[ P \cdot \frac{v}{R \cdot T} \right]$$

$$\ln [v_4] = \ln \left[ \frac{v}{v - b_M} \right] + \frac{b_4}{v - b_M} - \left[ \frac{\frac{2}{R}}{T^{1,5} \cdot b_M} \cdot \left( y_1 \cdot [a_4 \cdot 35]^{0,5} + y_2 \cdot [a_4 \cdot a_2]^{0,5} + y_3 \cdot [a_4 \right.$$

$$\cdot a_3]^{0,5} + y_4 \cdot a_4 + y_5 \cdot [a_4 \cdot 46]^{0,5} + y_6 \cdot [a_4 \cdot a_6]^{0,5} + y_7 \cdot [a_4 \cdot a_7]^{0,5} \cdot \ln \left( \frac{v + b_M}{v} \right) \right] + a_M$$

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$$\frac{R}{T^{1.5}} \cdot \frac{1}{b_M^2} \cdot \left[ \ln \left( \frac{v + b_M}{v} \right) - \left( \frac{b_M}{v + b_M} \right) \right] - \ln \left[ P \cdot \frac{v}{R \cdot T} \right]$$

$$\ln [v_5] = \ln \left[ \frac{v}{v - b_M} \right] + \frac{b_5}{v - b_M} - \left[ \frac{\frac{2}{R}}{T^{1.5} \cdot b_M} \cdot \left( y_1 \cdot [46 \cdot 35]^{0.5} + \frac{y_1}{2} \cdot R^2 \cdot T^{2.5} \cdot K + y_2 \cdot [46 \right.$$

$$\cdot a_2]^{0.5} + y_3 \cdot [46 \cdot a_3]^{0.5} + y_4 \cdot [46 \cdot a_4]^{0.5} + y_5 \cdot [46 + a_5] + y_6 \cdot [46 \cdot a_6]^{0.5} + y_7 \cdot [46$$

$$\cdot a_7]^{0.5} \cdot \ln \left( \frac{v + b_M}{v} \right) \right] + a_M \cdot \frac{\frac{R}{T^{1.5}}}{b_M^2} \cdot \left[ \ln \left( \frac{v + b_M}{v} \right) - \left( \frac{b_M}{v + b_M} \right) \right] - \ln \left[ P \cdot \frac{v}{R \cdot T} \right]$$

$$\ln [v_6] = \ln \left[ \frac{v}{v - b_M} \right] + \frac{b_6}{v - b_M} - \left[ \frac{\frac{2}{R}}{T^{1.5} \cdot b_M} \cdot \left( y_1 \cdot [a_6 \cdot 35]^{0.5} + y_2 \cdot [a_6 \cdot a_2]^{0.5} + y_3 \cdot [a_6 \right.$$

$$\cdot a_3]^{0.5} + y_4 \cdot [a_6 \cdot a_4]^{0.5} + y_5 \cdot [a_6 \cdot 46]^{0.5} + y_6 \cdot a_6 + y_7 \cdot [a_6 \cdot a_7]^{0.5} \cdot \ln \left( \frac{v + b_M}{v} \right) \right] + a_M$$

$$\frac{R}{T^{1.5}} \cdot \frac{1}{b_M^2} \cdot \left[ \ln \left( \frac{v + b_M}{v} \right) - \left( \frac{b_M}{v + b_M} \right) \right] - \ln \left[ P \cdot \frac{v}{R \cdot T} \right]$$

$$\ln [v_7] = \ln \left[ \frac{v}{v - b_M} \right] + \frac{b_7}{v - b_M} - \left[ \frac{\frac{2}{R}}{T^{1.5} \cdot b_M} \cdot \left( y_1 \cdot [a_7 \cdot 35]^{0.5} + y_2 \cdot [a_7 \cdot a_2]^{0.5} + y_3 \cdot [a_7 \right.$$

$$\cdot a_3]^{0.5} + y_4 \cdot [a_7 \cdot a_4]^{0.5} + y_5 \cdot [a_7 \cdot 46]^{0.5} + y_6 \cdot [a_7 \cdot a_6]^{0.5} + y_7 \cdot a_7 \cdot \ln \left( \frac{v + b_M}{v} \right) \right] + a_M$$

$$P = \frac{R}{T^{1.5}} \cdot \frac{1}{b_M^2} \cdot \left[ \ln \left( \frac{v + b_M}{v} \right) - \left( \frac{b_M}{v + b_M} \right) \right] - \ln \left[ P \cdot \frac{v}{R \cdot T} \right]$$

$$\log [f_s] = 3,8926 - \frac{494,34}{T} - \frac{461730}{T^2} + \frac{3,8535 \times 10^7}{T^3}$$

$$\log [P_w] = 6,0034 - \frac{2869,6}{T} + \frac{442350}{T^2} - \frac{7,6887 \times 10^7}{T^3}$$

$$v_w = \left[ 4,3257 - 0,033622 \cdot T + 0,00012464 \cdot T^2 - 2,0255 \times 10^{-7} \cdot T^3 + 1,2549 \times 10^{-10} \cdot T^4 \right] \cdot \frac{18,016}{1000}$$

$$f_w = f_s \cdot \exp \left[ \frac{v_w}{8314,3 \cdot T} \cdot (P - P_w) \cdot 10^5 \right]$$

$$f_1 = v_1 \cdot y_1 \cdot P$$

$$f_w = f_1$$

$$F = 0,1 \quad \text{Relación molar de agua líquida de entrada a gas y a una } T = 273,15 + 60 \text{ para el agua líquida de quench}$$

$$\begin{aligned} \text{Entrada} = & y_{0,1} \cdot h ['H_2O'; T=500] + y_{0,2} \cdot h ['CH_4'; T=500] + y_{0,3} \cdot h ['H_2'; T=500] + y_{0,4} \\ & \cdot h ['CO'; T=500] + y_{0,5} \cdot h ['CO_2'; T=500] + y_{0,6} \cdot h ['N_2'; T=500] + y_{0,7} \cdot h ['Argon'; T=500; P=1] \\ & + F \cdot [h ('H_2O'; T=273,15 + 60) + h ('Water'; T=273,15 + 60; x=0) - h ('Water'; T=273,15 + 60; x=1)] \end{aligned}$$

### Composición gaseosa

$$y_1 = \frac{y_{0,1} + x}{1 + x} \quad H_2O$$

$$y_2 = \frac{y_{0,2}}{1 + x} \quad CH_4$$

$$y_3 = \frac{y_{0,3}}{1 + x} \quad H_2$$

$$y_4 = \frac{y_{0,4}}{1 + x} \quad CO$$

$$y_5 = \frac{y_{0,5}}{1 + x} \quad CO_2$$

$$y_6 = \frac{y_{0,6}}{1 + x} \quad N_2$$

$$y_7 = \frac{y_{0,7}}{1 + x} \quad A$$

$$\begin{aligned} \text{Salida} = & [y_1 \cdot h ('H_2O'; T=T) + y_2 \cdot h ('CH_4'; T=T) + y_3 \cdot h ('H_2'; T=T) + y_4 \cdot h ('CO'; T=T) + y_5 \\ & \cdot h ('CO_2'; T=T) + y_6 \cdot h ('N_2'; T=T) + y_7 \cdot h ('Argon'; T=T; P=1) + \Delta h] \cdot [1 + x] + [F - x] \\ & \cdot [h ('H_2O'; T=T) + h ('Water'; T=T; x=0) - h ('Water'; T=T; x=1)] \end{aligned}$$

$$\text{Entrada} = \text{Salida} \quad \text{El proceso de mezcla y obtención del equilibrio líquido-vapor es adiabático}$$

### SOLUTION

Unit Settings: [kJ]/[K]/[bar]/[kmol]/[degrees]

$$a_M = 38,43$$

$$\Delta h = -464,4 \quad [kJ/kmol]$$

$$DT = -0,0833$$

$$F = 0,1$$

$$f_s = 8,909$$

$$K = 0,001821$$

$$P_w = 9,565 \quad [bar]$$

$$\text{Salida} = -157848 \quad [kJ/kmol]$$

$$v = 1,205$$

$$x = 0,02981$$

$$b_M = 0,0188$$

$$dK = -0,003078$$

$$\text{Entrada} = -157848 \quad [kJ/kmol]$$

$$f_1 = 9,008$$

$$f_w = 9,008$$

$$P = 30 \quad [atm]$$

$$R = 0,08206$$

$$T = 451,3 \quad [K]$$

$$v_w = 0,02028$$

**Arrays Table**

	$a_i$	$b_i$	$y_i$	$v_i$	$y_{0,i}$
1	167,7	0,0146	0,3401	0,883	0,3204
2	31,57	0,0296	0,001733	1,018	0,001785
3	1,768	0,01571	0,3852	1,043	0,3967
4	17,02	0,02741	0,003302	1,029	0,0034
5	15,45	0,0297	0,1434	0,9852	0,1477
6	15,46	0,02678	0,126	1,031	0,1298
7	16,86	0,0224	0	1,025	0

**Parametric Table: Table 2**

	T	$f_1$	$f_w$
	[K]		
Run 1	450	8,843	8,743
Run 2	450,1	8,845	8,765
Run 3	450,2	8,847	8,787
Run 4	450,3	8,849	8,808
Run 5	450,4	8,852	8,83
Run 6	450,6	8,854	8,852
Run 7	450,7	8,856	8,874
Run 8	450,8	8,859	8,896
Run 9	450,9	8,861	8,918
Run 10	451	8,863	8,94